

Edge and Connected Edge domination number of Complement of $B(\overline{K_p}, \overline{L(G)}, \text{NINC})$

Dr. S. Muthammai

Principal(Retd.), Alagappa Government Arts college, Karaikudi, Tamil Nadu, India.

muthammai .sivakami @ gmail.com,

S. Dhanalakshmi

Government Arts College for Women (Autonomous), Pudukkottai, Tamil Nadu, India.

dhanalakshmi8108@gmail.com

Abstract

For any graph G , let $V(G)$ and $E(G)$ denote the vertex set and edge set of G respectively. The Boolean function graph $B(\overline{K_p}, \overline{L(G)}, \text{NINC})$ of G is a graph with vertex set $V(G) \cup E(G)$ and two vertices in $B(\overline{K_p}, \overline{L(G)}, \text{NINC})$ are adjacent if and only if they correspond to two non adjacent edges of G or to a vertex and an edge not incident to it in G . For brevity, this graph is denoted by $B_3(G)$. In this paper, edge domination numbers of Complement of Boolean Function Graph $B(\overline{K_p}, \overline{L(G)}, \text{INC})$ of some standard graphs and corona graphs are obtained.

Keywords: Boolean Function graph, Edge Domination Number.

1. Introduction

Graphs discussed in this paper are undirected and simple graphs. For a graph G , let $V(G)$ and $E(G)$ denote its vertex set and edge set respectively. A graph with p vertices and q edges is denoted by $G(p, q)$. A subset $F \subseteq E(G)$ is called an edge dominating set of G , if every edge not in F is adjacent to some edge in F . The edge domination number $\gamma'(G)$ of G is the minimum cardinality taken over all edge dominating sets of G . The concept of edge domination was introduced by Mitchell and Hedetaiemi[8] and it was studied by Arumugam and Velammal[1]. Complementary edge domination in graphs is studied by Kulli and Soner [7] Jayaram[6] studied the line dominating sets and obtained bounds for the line domatic number. The corona $G_1 \circ G_2$ of two graphs G_1 and G_2 is defined as the graph obtained by taking one copy of G_1 (which has p_1 vertices) and p_1 copies of G_2 , and then joining the i^{th} vertex of G_1 to every vertex of in the i^{th} copy of G_2 . For any graph G , $G \circ K_1$ is denoted by G^+ .

An edge dominating set F of G is called a connected edge dominating set of G , if the induced subgraph $\langle F \rangle$ is connected. The connected edge domination number $\gamma'_c(G)$ of G is the minimum cardinality taken over all connected edge dominating sets of G .

Janakiraman et al., introduced the concept of Boolean function graphs [3 - 5]. For any graph G , let $V(G)$ and $E(G)$ denote the vertex set and edge set of G respectively. The Boolean function graph $B(\overline{K_p}, \overline{L(G)}, \text{NINC})$ of G is a graph with vertex set $V(G) \cup E(G)$ and two vertices in $B(\overline{K_p}, \overline{L(G)}, \text{NINC})$ are adjacent if and only if they correspond to two non adjacent edges of G or to a vertex and an edge not incident to it in G . For brevity, this graph is denoted by $B_3(G)$.

In this paper, edge domination numbers of Complement of $B(K_p, L(G), \text{INC})$ of some standard graphs are obtained.

2. Prior Results

Observation 2.1. [5]

Let G be a graph with p vertices and q edges.

1. If G has p vertices, then the complete graph on p vertices is an induced subgraph of $\overline{B_3(G)}$. Also $L(G)$ is an induced subgraph.
2. The degree of a vertex $v \in V(G)$ in $\overline{B_3(G)}$ is $p-1+\text{deg}_G(v)$ and the degree of a vertex e' of $L(G)$ in $\overline{B_3(G)}$ is $\text{deg}_{L(G)}(e')+2$ and hence $\Delta(\overline{B_3(G)}) = p-1+ \Delta(G)$ and $\delta(\overline{B_3(G)}) = \delta'(G) + 2$, where $\delta'(G) = \delta(L(G))$.
3. $\overline{B_3(G)}$ is a connected graph, for any graph G .

3. Main Results

In the following, edge domination numbers of $\overline{B_3(P_n)}$, $\overline{B_3(C_n)}$, $\overline{B_3(K_{1,n})}$ and corona graphs are found and the bounds are obtained.

Theorem 3.1: For the Path P_n on n ($n \geq 3$) vertices, $\gamma'(\overline{B_3(P_n)}) = n- 1$.

Proof: Let v_1, v_2, \dots, v_n be the vertices and e_1, e_2, \dots, e_{n-1} be the edges in P_n , where $e_i = (v_i, v_{i+1})$ $i = 1, 2, \dots, n-1$. Then $v_1, v_2, \dots, v_n, e_1, e_2, \dots, e_{n-1} \in V(\overline{B_3(P_n)})$. $\overline{B_3(P_n)}$ has $2n-1$ vertices and $((n^2+ 5n-8)/2)$ edges. Let $D' = \bigcup_{i=1}^{n-1} \{(v_i, e_i)\}$. Then $D' \subseteq E(\overline{B_3(P_n)})$. Each edge in $V(\overline{B_3(P_n)}) - D'$ adjacent to atleast one edge in D' . Therefore, D' is an edge dominating set of $\overline{B_3(P_n)}$. Hence, $\gamma'(\overline{B_3(P_n)}) \leq |D'| = n - 1$. Let D'' be an edge dominating set of $\overline{B_3(P_n)}$. To

dominate edges of the form (v_i, e_i) , $(i = 1, 2, \dots, n-1)$ and (v_{i+1}, e_i) , $i = 1, 2, \dots, n-1$. D'' contains atleast $(n-1)$ edges. These $(n-1)$ edges dominate edges of K_n and $L(P_n)$ in $\overline{B_3(P_n)}$. Therefore, $|D''| \geq n-1$. Hence, $\gamma'(\overline{B_3(P_n)}) = n-1$.

Remark:

1. $\gamma'(\overline{B_3(C_n)}) = n, n \geq 4$
2. $\gamma'(\overline{B_3(K_{1,n})}) = n, n \geq 3$.

Theorem 3.2: For the path P_n on n ($n \geq 3$) vertices, $\gamma'(\overline{B_3(P_n^+)}) = 2n-1$.

Proof: Let $V(P_n^+) = \{v_1, v_2, \dots, v_n, u_1, u_2, \dots, u_n\}$, where v_1, v_2, \dots, v_n are the vertices of P_n and u_1, u_2, \dots, u_n are the pendant vertices of P_n^+ and $e_i = (v_i, v_{i+1})$ $i = 1, 2, \dots, n-1$ and $f_i = (v_i, u_i)$, $i = 1, 2, \dots, n$ be the edges of P_n^+ . Then $v_1, v_2, \dots, v_n, u_1, u_2, \dots, u_n, e_1, e_2, \dots, e_{n-1}, f_1, f_2, \dots, f_n \in \overline{B_3(P_n^+)}$. $\overline{B_3(P_n^+)}$ has $4n-1$ vertices and $(2n^2 + 6n - 6)$ edges.

Let $F_1 = \bigcup_{i=1}^{n-1} \{(v_i, e_i)\}$ and $F_2 = \bigcup_{i=1}^n \{(u_i, f_i)\}$ and let $D' = F_1 \cup F_2 \subseteq E(\overline{B_3(P_n^+)})$.

$|D'| = n-1 + n = 2n-1$. F_1 dominates edges of $L(P_n)$ and edges of the form (e_i, f_i) , $i = 1, 2, \dots, n-1$ and (e_i, f_{i+1}) , $i = 1, 2, \dots, n-1$. $F_1 \cup F_2$ dominates edges of K_{2n-1} in $\overline{B_3(P_n^+)}$. Therefore, F is an edge dominating set of $\overline{B_3(P_n^+)}$ and as in Theorem 1, F is minimum. D' is a minimum edge dominating set of $\overline{B_3(P_n^+)}$. Hence, $\gamma'(\overline{B_3(P_n^+)}) = 2n-1$.

Remark: $\gamma'(\overline{B_3(C_n^+)}) = 2n, n \geq 4$.

Theorem 3.3: For the star $K_{1,n}$ on $n+1$ vertices, $\gamma'(\overline{B_3(K_{1,n}^+)}) = 2n+1, n \geq 3$.

Proof: Let $V(K_{1,n}^+) = \{v, v_1, v_2, \dots, v_n, u, u_1, u_2, \dots, u_n\}$, where v is the central vertex and $\langle \{v_1, v_2, \dots, v_n\} \rangle \cong K_{1,n}$ and u_1, u_2, \dots, u_n are the pendant vertices of $K_{1,n}^+$ and $e_i = (v, v_i)$ $i = 1, 2, \dots, n$ and $f = (v, u)$, $f_i = (v_i, u_i)$ $i = 1, 2, \dots, n$ be the edges of $K_{1,n}^+$. Then $v, v_1, v_2, \dots, v_n, u, u_1, u_2, \dots, u_n, e_1, e_2, \dots, e_n, f_1, f_2, \dots, f_n \in \overline{B_3(K_{1,n}^+)}$. $\overline{B_3(K_{1,n}^+)}$ has $(4n+1)$ vertices and $((5n^2 + 15n + 4)/2)$ edges.

Let $F_1 = \bigcup_{i=1}^n \{(v_i, u_i)\}$ $F_2 = \bigcup_{i=1}^n \{(e_i, f_i)\}$ and $F_3 = \{(v, f)\}$.

Let $D' = F_1 \cup F_2 \cup F_3 \subseteq E(\overline{B_3(K_{1,n}^+)})$. $|D'| = n + n + 1 = 2n + 1$. $F_1 \cup F_3$ dominates all the edges of K_{2n+2} induced by $v, v_1, \dots, v_n, u, u_1, \dots, u_n$ and edges of the form $(v_i, e_i), (v_i, f_i), (u_i, f_i)$ ($i = 1, 2, \dots, n$) and (u, f) . F_2 dominates the edges of $L(K_{1,n}^+)$. Therefore, F is an edge dominating set of $\overline{B_3(K_{1,n}^+)}$ and is minimum. Hence, $\gamma'(\overline{B_3(K_{1,n}^+)}) = 2n + 1, n \geq 3$.

Theorem 3.4: Let G be a (p, q) graph with $p \geq 3$. Then

- (i) $\gamma'(\overline{B_3(G)}) \leq \gamma'(K_p) + \gamma'(L(G))$.
- (ii) $\gamma'(\overline{B_3(G)}) \leq \max(p, q)$, if $\delta(G) \geq 1$.

Proof:

(i) Since K_p and $L(G)$ are induced subgraphs of $\overline{B_3(G)}$, $\gamma'(\overline{B_3(G)}) \leq \gamma'(K_p) + \gamma'(L(G))$.

(ii) **Case 1:** $p \geq q$.

Since $\delta(G) \geq 1$, G has no isolated vertices and each vertex in G is incident with atleast one edge in G .

Let v_1, v_2, \dots, v_p be the p vertices of G and e_i be incident with v_i , for $i=1, 2, \dots, p$.

Then $(v_i, e_i) \in E(\overline{B_3(G)})$, $i = 1, 2, \dots, p$ and $\{(v_i, e_i) / i=1, 2, \dots, p\}$ is an edge dominating set of $\overline{B_3(G)}$ and $\gamma'(\overline{B_3(G)}) \leq p$.

Case 2: $p < q$.

Let e_1, e_2, \dots, e_q be the edges in G and v_j be incident with e_j , $j = 1, 2, \dots, q$.

Then $\{(v_i, e_i) / i=1, 2, \dots, q\}$ is an edge dominating set of $\overline{B_3(G)}$ and $\gamma'(\overline{B_3(G)}) \leq q$.

Therefore, $\gamma'(\overline{B_3(G)}) \leq \max(p, q)$.

In the following, the graphs for which $\gamma'(\overline{B_3(G)}) = 1, 2$ (or) 3 are characterized.

Observation 3.1: $\gamma'(\overline{B_3(G)}) = 1$ if and only if G is one of the following graphs: $2K_1, 3K_1, K_2$ and $K_2 \cup K_1$.

Theorem 3.5: $\gamma'(\overline{B_3(G)}) = 2$ if and only if G is one of the following graphs: $P_3, C_3, 4K_1, K_2 \cup 2K_1, P_3 \cup K_1, 2K_2, 5K_1, K_2 \cup 3K_1$ and $2K_2 \cup K_1$.

Proof:

Case 1: G contains no isolated vertices.

If G contains C_4 as a subgraph, then $\gamma'(\overline{B_3(G)}) \geq 4$, since $\gamma'(\overline{B_3(C_4)}) = 4$.

If G contains $K_{1,3}$ as a subgraph, then $\gamma'(\overline{B_3(G)}) \geq 3$, since $\gamma'(\overline{B_3(K_{1,3})}) = 3$.

If G contains P_4 as a subgraph, then $\gamma'(\overline{B_3(G)}) \geq 3$, since $\gamma'(\overline{B_3(P_4)}) = 3$.

Therefore, G is one of the graphs $K_2, P_3, C_3, 2K_2$ and $P_3 \cup K_2$. But, $\gamma'(\overline{B_3(K_2)}) = 1$ and $\gamma'(\overline{B_3(P_3 \cup K_2)}) = 3$. Hence, $G \cong P_3, C_3$ (or) $2K_2$.

Case 2: G contains isolated vertices.

If $G \cong nK_1, n \geq 6$, then $\gamma'(\overline{B_3(G)}) \geq 3$, since K_6 is an induced subgraph of $\overline{B_3(G)}$ and $\gamma'(K_6) = 3$. If $G = 2K_1$ (or) $3K_1$, then $\gamma'(\overline{B_3(G)}) = 1$. Therefore, $G \cong 4K_1$ (or) $5K_1$.

Let G be not totally connected. Then G contains atleast one edge and $\delta(G) \geq 0$. If $G \cong K_2 \cup mK_1, m \geq 4$ (or) $P_3 \cup K_1, 2K_2 \cup nK_1$ for $n \geq 2$, then $\gamma'(\overline{B_3(G)}) \geq 3$. Therefore, $G \cong K_2 \cup 2K_1, K_2 \cup 3K_1, P_3 \cup K_1$ (or) $2K_2 \cup K_1$. If $G \cong C_3 \cup K_1$, then $\gamma'(\overline{B_3(G)}) = 3$.

From Case 1 and Case 2, G is one of the following graphs: $P_3, C_3, 2K_2, 4K_1, 5K_1, K_2 \cup 2K_1, K_2 \cup 3K_1, P_3 \cup K_1$ and $2K_2 \cup K_1$. Conversely, if G is one of the graphs given above, $\gamma'(\overline{B_3(G)}) = 2$.

In the same way, the following theorem can be proved.

Theorem 3.6: $\gamma'(\overline{B_3(G)}) = 3$ if and only if G is one of the following graphs: $6K_1, 7K_1, K_2 \cup 4K_1, K_2 \cup 5K_1, P_3 \cup 2K_1, C_3 \cup K_1, C_3 \cup 2K_1, P_4 \cup K_1, K_{1,3} \cup K_1, P_3 \cup K_2, P_4, K_{1,3}$ and $K_4 - e$.

4. Connected edge domination number of $\overline{B_3(G)}$

In the following, Connected edge domination numbers of $\overline{B_3(P_n)}, \overline{B_3(C_n)}, \overline{B_3(K_{1,n})}$ are found and an upperbound is obtained.

Theorem 4.1: For the path $P_n (n \geq 4)$ on n vertices, $\gamma_c'(\overline{B_3(P_n)}) = \left\lfloor \frac{3n-3}{2} \right\rfloor$.

Proof:

Case 1: n is odd.

Let $A_1 = \bigcup_{i=1}^{n-2} \{(v_i, v_{i+1})\}$, $A_2 = \bigcup_{i=1}^{(n-1)/2} \{(v_{2i-1}, e_{2i-1})\}$ and $A_3 = \{(v_{n-1}, e_{n-1})\}$.

Let $A = A_1 \cup A_2 \cup A_3$ and $|A| = (3n-3)/2$. The set A_1 dominates all the edges of K_n in $\overline{B_3(P_n)}$. The set $A_2 \cup A_3$ dominates all the edges of $L(P_n)$ and the edges of the form (v, e) in $\overline{B_3(P_n)}$. Therefore A is an edge dominating set of $\overline{B_3(P_n)}$. Also, $\langle A \rangle$ is a tree obtained from P_{n-1} by attaching a pendant edge at v_{2i-1} ($i = 1, 2, \dots, (n-1)/2$) and at v_{n-1} . Therefore, A is a connected edge dominating set of $\overline{B_3(P_n)}$ and $\gamma_c'(\overline{B_3(P_n)}) \leq |A| = ((3n-3)/2)$.

Let D' be a minimum edge dominating set of $\overline{B_3(P_n)}$. Since $\gamma_c'(K_n) = n-2$, to dominate edges of K_n in $\overline{B_3(P_n)}$, D' contains $(n-2)$ edges. These edges dominate the edges of the form (v, e) in $\overline{B_3(P_n)}$. To dominate edges of $L(P_n)$ and to maintain connectedness of $\langle D' \rangle$, atleast $((n+1)/2)$ edges are to be added to D' . Therefore, D' contains atleast $(n-2) + ((n+1)/2) = ((3n-3)/2)$ edges.

Hence, $\gamma_c'(\overline{B_3(P_n)}) \geq ((3n-3)/2)$

Case 2: n is even.

Let $A_4 = \bigcup_{i=1}^{n/2} \{(v_{2i-1}, e_{2i-1})\}$. Then the set $A_1 \cup A_4$ is an minimum edge dominating set of $\overline{B_3(P_n)}$ and $\langle A_1 \cup A_4 \rangle$ is a tree obtained from P_{n-1} by attaching pendant edge at v_{2i-1} , $i = 1, 2, \dots, (n/2)$. Therefore, $A_1 \cup A_4$ is a connected edge dominating set of $\overline{B_3(P_n)}$. As in Case1, $A_1 \cup A_4$ is minimum. Hence, $\gamma_c'(\overline{B_3(P_n)}) = |A_1 \cup A_4| = (n-2) + n/2 = (3n-4)/2 = \lfloor \frac{3n-3}{2} \rfloor$.

By Case 1 and Case 2, $\gamma_c'(\overline{B_3(P_n)}) = \lfloor \frac{3n-3}{2} \rfloor, n \geq 4$.

Observation: $\gamma_c'(\overline{B_3(P_3)}) = 2$.

Theorem 4.2: For the cycle C_n ($n \geq 3$) on n vertices, $\gamma_c'(\overline{B_3(C_n)}) = \lfloor \frac{3n-1}{2} \rfloor$.

Proof: Let $D_1 = \bigcup_{i=1}^{n-1} \{(v_i, v_{i+1})\}$

Case 1: n is odd.

Let $D_2 = \bigcup_{i=1}^{(n+1)/2} \{(v_{2i-1}, u_{2i-1})\}$. Then the set $D_1 \cup D_2$ is an edge dominating set of $\overline{B_3(C_n)}$ and

$\langle D_1 \cup D_2 \rangle$ is a tree obtained from by attaching a pendant edge at v_i , $i=1, 2, \dots, (n+1)/2$.

Therefore, $D_1 \cup D_2$ is a connected edge dominating set of $\overline{B_3(C_n)}$ and is minimum, as in Case 1 of Theorem 4.1.

$$\text{Hence, } \gamma_c'(\overline{B_3(C_n)}) = |D_1 \cup D_2| = (n-1) + ((n+1)/2) = (3n-1)/2.$$

Case 2: n is even.

Let $D_3 = \bigcup_{i=1}^{n/2} \{(v_{2i-1}, u_{2i-1})\}$. Then the set $D_1 \cup D_3$ is an edge dominating set of $\overline{B_3(C_n)}$ and $\langle D_1 \cup D_3 \rangle$ is a tree obtained from P_n by attaching a pendant edge at $v_i, i=1, 2, \dots, (n/2)$.

Therefore, $D_1 \cup D_3$ is a connected edge dominating set of $\overline{B_3(C_n)}$ and is minimum.

$$\text{Hence, } \gamma_c'(\overline{B_3(C_n)}) = |D_1 \cup D_3| = (n-1) + (n/2) = (3n-2)/2 = \left\lfloor \frac{3n-1}{2} \right\rfloor.$$

$$\text{By Case 1 and Case 2, } \gamma_c'(\overline{B_3(C_n)}) = \left\lfloor \frac{3n-1}{2} \right\rfloor, n \geq 3.$$

Theorem 4.3: For the star $K_{1,n}$ ($n \geq 3$) on $(n+1)$ vertices, $\gamma_c'(\overline{B_3(K_{1,n})}) = 2n-1$.

Proof: Let $F_1 = \bigcup_{i=1}^{n-2} \{(v_i, v_{i+1})\}$, $F_2 = (\bigcup_{i=1, i \neq 2}^n \{(v_i, e_i)\})$, $F_3 = \{(v, v_1), (v, e_n)\}$.

Then the set $F_1 \cup F_2 \cup F_3$ is an edge dominating set of $\overline{B_3(K_{1,n})}$ and

$\langle F_1 \cup F_2 \cup F_3 \rangle$ is a tree obtained from P_n by attaching a pendant edge at all vertices, except at v_2 . Therefore, $F_1 \cup F_2 \cup F_3$ is a connected edge dominating set of $\overline{B_3(K_{1,n})}$ and is minimum.

$$\text{Hence, } \gamma_c'(\overline{B_3(K_{1,n})}) = |F_1 \cup F_2 \cup F_3| = (n-2) + (n-1) + 2 = 2n-1.$$

Theorem 4.4: Let G be a connected (p, q) graph. Then $\gamma_c'(\overline{B_3(G)}) \leq p-1 + \alpha_0(L(G))$.

Proof: K_p is an induced subgraph of $\overline{B_3(G)}$. Let T be a spanning tree in K_p , $|E(T)| = p-1$. Let D be a minimum point cover of $L(G)$. Then, $|D| = \alpha_0(L(G))$. Assume $D = \{e_1, e_2, \dots, e_k\}$, where $k = \alpha_0(L(G))$ and let $e_i \in E(G)$ be incident with $v_i \in E(G)$, $i = 1, 2, \dots, k$. Then $(v_i, e_i) \in \overline{B_3(G)}$, $i = 1, 2, \dots, k$ and the set $\{(v_i, e_i) / i=1, 2, \dots, k\} \cup E(T)$ is a connected edge dominating set of $\overline{B_3(G)}$. Therefore, $\gamma_c'(\overline{B_3(G)}) \leq k + p-1 = p-1 + \alpha_0(L(G))$.

Equality holds, if $G \cong C_n, n \geq 3$. Since $\alpha_0(L(C_n)) = \alpha_0(L(C_n)) = \left\lfloor \frac{n}{2} \right\rfloor$.

Remark:

1. If $\gamma_c'(\overline{B_3(G)}) = 2$ if and only if $G \cong P_3$.
2. If $\gamma_c'(\overline{B_3(G)}) = 3$ if and only if $G \cong K_{1,2}$ (or) P_3 .

5. Conclusion

In this paper, Edge and Connected edge domination numbers of $B(\overline{K_p}, \overline{L(G)})$, NINC) of path, cycle, stars and corona graphs are obtained.

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